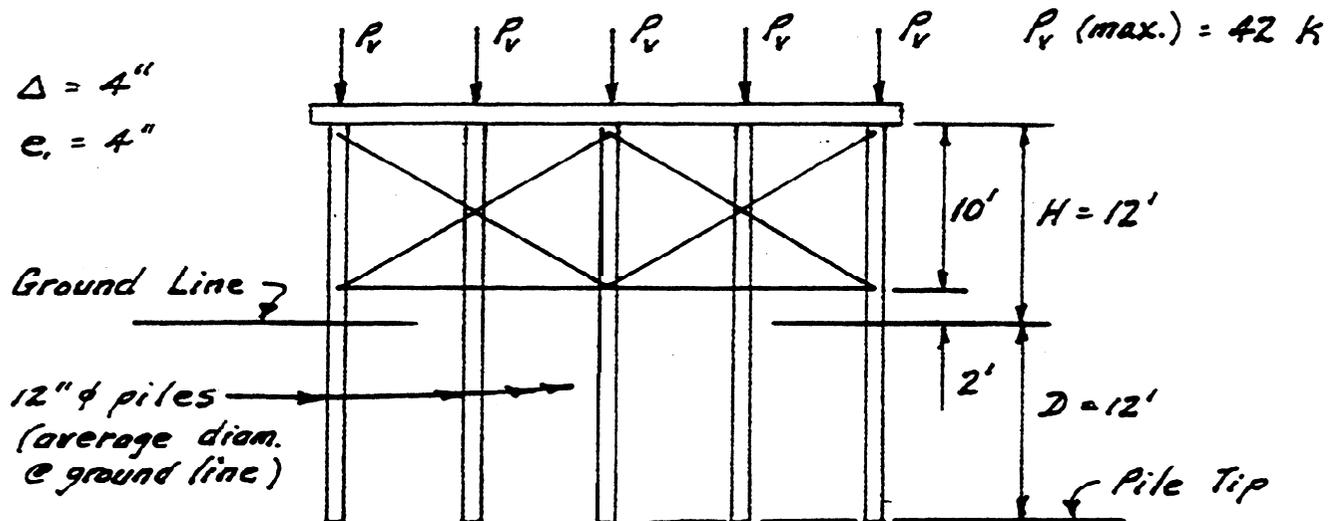


## EXAMPLE 14

### Investigate Adequacy of Timber Pile Bent Design

#### Example 14A (Type I Bent)



#### Preliminary Calculations and Assumptions

##### 1. Pile properties (12" $\phi$ pile; $r = 6''$ )

$$A = \pi r^2 = 113 \text{ in}^2$$

$$S = \frac{\pi r^3}{4} = 170 \text{ in}^3$$

$$I = \frac{\pi r^4}{4} = 1018 \text{ in}^4$$

##### 2. Required Pile Penetration (Section 7-3.02A)

$$\text{Minimum } D/H = 0.75 ; \text{ design } D/H = 12/12 = 1.0 \quad \text{OK}$$

$$\text{Minimum } D \text{ for construction} = (0.75 \times 12.0) = 9.0'$$

##### 3. Soil Relaxation Factor (Section 7-3.02D)

Assume average soil and 30-day time period.

From Soil Factor Chart (Fig. 7-10)  $R = 1.25$

##### 4. Point of Pile Fixity (Section 7-3.02B)

$$Y_1 = (\bar{A}) \times (\text{pile diam. @ ground line}) = (4 \times 1.0) = 4.0'$$

$$Y_2 = (Y_1) \times (\text{soil relax. factor}) = (4.0 \times 1.25) = 5.0'$$

## Preliminary Calculations Continued

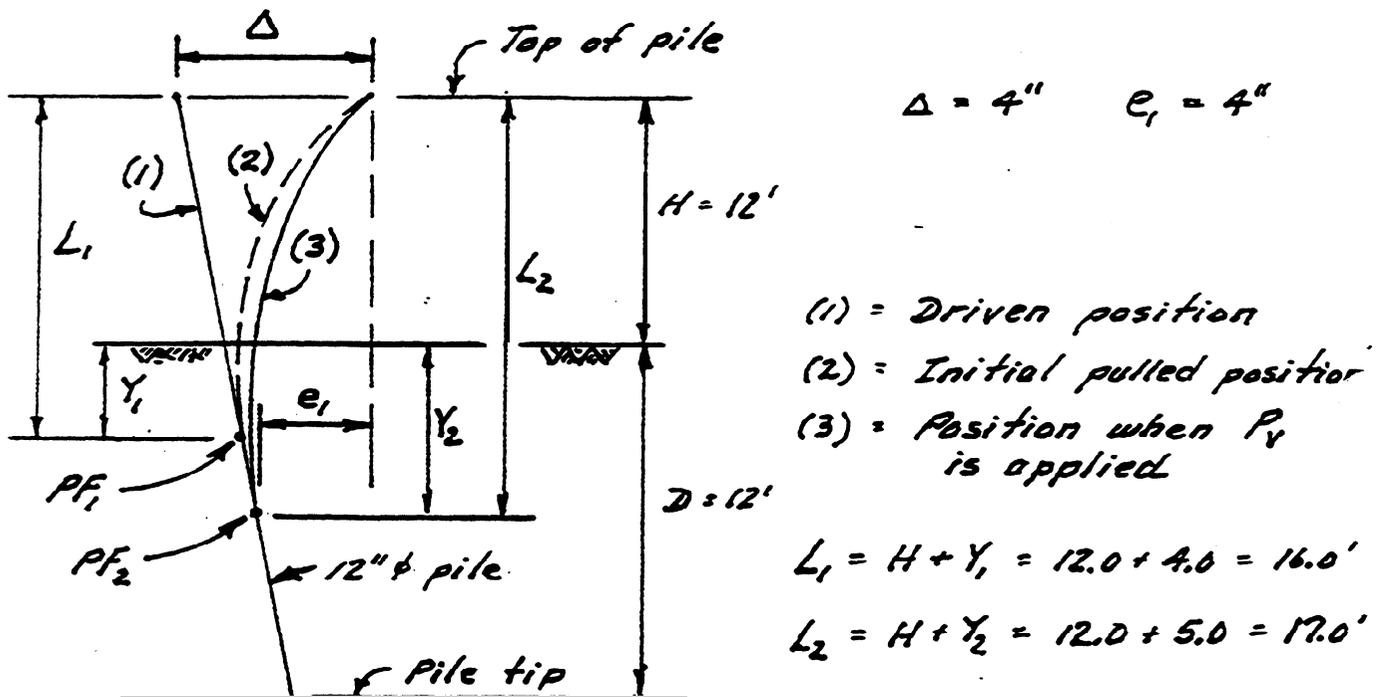
### 5. Driving Tolerances (Section 7-3.02C)

Max. pile pull =  $\Delta = 4''$   
Max. pile lean =  $e_1 = 4''$  } Values from F/W drawings

### 6. Modulus of Elasticity (Section 7-3.02E)

Assume  $E = 1,600,000$  psi

### Investigate Effect of Pile Pull



### Pile Schematic (no scale)

1. Calculate  $F_1$  = force to pull pile into line

$$F_1 = \frac{3EI\Delta}{(12L)^3} = \frac{3(1.6 \times 10^6)(1010)(4)}{(12 \times 16.0)^3} = 2762 \text{ lbs.}$$

2. Calculate the initial bending stress

$$f_{bpl} = \frac{F_1(12L)}{S} = \frac{(2762)(12 \times 16)}{170} = 3119 \text{ psi}$$

3119 psi < 4000 psi allowed. OK

## Pile Pull Continued

3. Calculate  $F_2$  = force after soil relaxes

$$F_2 = \frac{F_1 (L_1)^3}{(L_2)^3} = \frac{2762 (16.0)^3}{(17.0)^3} = 2303 \text{ lbs.}$$

4. Calculate final bending stress

$$f_{bp(2)} = \frac{F_2 (12L_2)}{S} = \frac{2303 (12 \times 17.0)}{170} = 2762 \text{ psi}$$

## Evaluate System Adequacy (Section 7-3.03E)

1. Determine bent type

$$L_u = Y_2 + (12.0 - 10.0) = 5.0 + 2.0 = 7.0'$$

$$L_u/d = \frac{7.0}{1.0} = 7 < 8 ; \therefore \text{Type I bent}$$

Do not consider design H (Section 7-3.03C)

2. Calc. stress due to vertical load eccentricity

$$f_{be(1)} = \frac{(P_v Y_e)}{S} = \frac{(42000)(4)}{170} = 988 \text{ psi}$$

3. Calc. stress due to axial compression

$$f_c = \frac{P_v}{A} = \frac{42000}{113} = 372 \text{ psi}$$

4. Determine allowable compressive stress

Note: bent supported at the cap in the longitudinal direction.

$$L_u \text{ (in longitudinal direction)} = L_2 = 17.0'$$

$$\text{Equivalent "d"} = \sqrt{A} = \sqrt{113} = 10.6''$$

$$L_u/d = \frac{17.0 \times 12}{10.6} = 19.25$$

$$F_c'' = \frac{480,000}{(19.25)^2} = 1295 \text{ psi}$$

## System Adequacy Continued

5. Solve combined stress expression

$$\frac{f_{bp(2)} + 2f_{bc(1)}}{3F_b} + \frac{2f_c}{3F_c} \neq 1.0$$

$$\frac{2762 + 2(988)}{3(1800)} + \frac{2(372)}{3(1295)}$$

$$0.88 + 0.19 = 1.07 > 1.0$$

System fails !!

Options available to make system adequate:

- (a) use larger diameter pile
- (b) reduce allowable values for  $\Delta$  and/or  $e_1$
- (c) shorten F/W span to reduce  $P_v$

Contractor resubmits design using 14"  $\phi$  piles.

<u>New pile properties</u>	<u>New design values</u>
$A = 154 \text{ in}^2$	$Y_1 = (4 \times \frac{1}{12}) = 4.67'$
$S = 269 \text{ in}^3$	$Y_2 = (1.25 \times 4.67) = 5.83'$
$I = 1886 \text{ in}^4$	$L_1 = H + 4.67 = 16.67'$
	$L_2 = H + 5.83 = 17.83'$

### Investigate Effect of Pile Pull

(Refer to sketch on page D-14-2 and previous calcs.)

$$F_1 = \frac{3EI\Delta}{(12L_1)^3} = \frac{3(1.6 \times 10^6)(1886)(4)}{(12 \times 16.67)^3} = 4524 \text{ lbs.}$$

$$f_{bp(1)} = \frac{F_1(12L_1)}{S} = \frac{(4524)(12 \times 16.67)}{269} = 3364 \text{ psi}$$

$$3364 < 4000 \text{ psi allowable} \quad \underline{\underline{OK}}$$

$$F_2 = \frac{F_1(L_1)^3}{(L_2)^3} = \frac{(4524)(16.67)^3}{(17.83)^3} = 3697 \text{ lbs.}$$

$$f_{bp(2)} = \frac{F_2(12L_2)}{S} = \frac{(3697)(12 \times 17.83)}{269} = 2941 \text{ psi}$$

## Evaluate System Adequacy

Check bent type -

$$L_u = \text{new } L_2 + (12.0 - 10.0) = 5.83 + 2.0 = 7.83'$$

$$L_u/d = \frac{(7.83)(12)}{14} = 6.71 < 8 \quad \underline{\underline{\text{still Type I bent}}}$$

$$f_{be(1)} = \frac{(P_v)(e_1)}{S} = \frac{(42000)(4)}{269} = 625 \text{ psi}$$

$$f_c = \frac{P_v}{A} = \frac{42000}{154} = 273 \text{ psi}$$

Allowable  $F_c$  -

$$L_u \text{ (longitudinal direction governs)} = L_2 = 17.83'$$

$$\text{Equivalent "d"} = \sqrt{154} = 12.4''$$

$$L_u/d = \frac{17.83 \times 12}{12.4} = 17.25$$

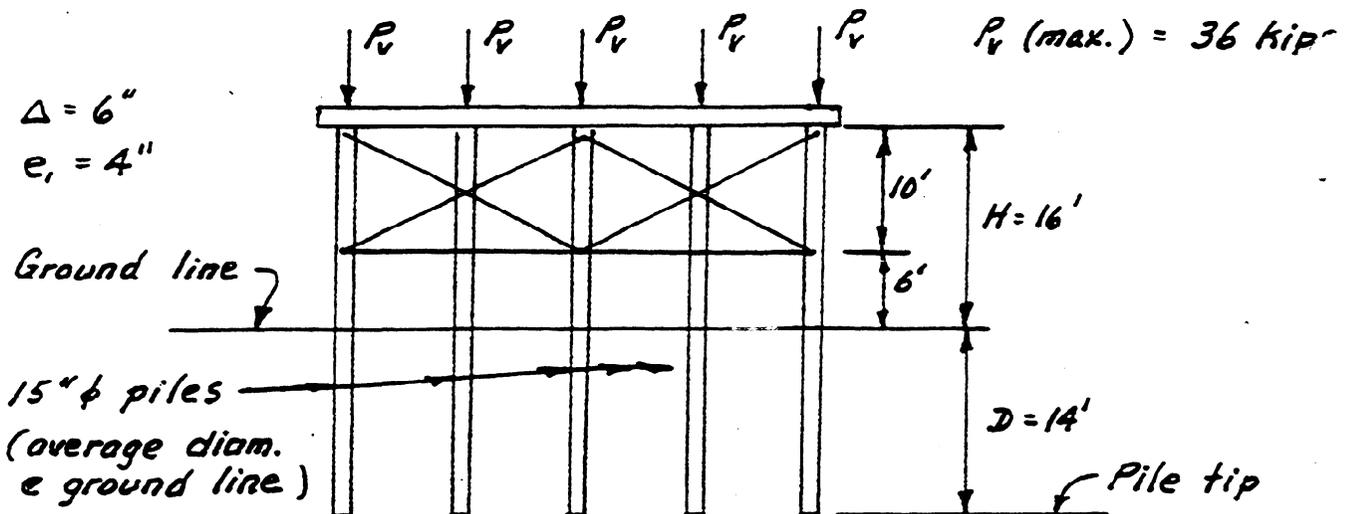
$$F_c = \frac{420000}{(17.25)^2} = 1613 \text{ psi} > 1600 \text{ psi} \quad \swarrow \text{use}$$

Solve combined stress expression -

$$\begin{aligned} \frac{f_{b(2)} + 2f_{be(1)}}{3F_b} + \frac{2f_c}{3F_c} &= \frac{2941 + 2(625)}{3(1800)} + \frac{2(273)}{3(1600)} \\ &= 0.78 + 0.11 = 0.89 < 1.0 \end{aligned}$$

System is now adequate

## Example 14B (Type II Bent)



### Preliminary Calculations and Assumptions

#### 1. Pile properties (15" $\phi$ pile; $r = 7.5''$ )

$$A = \pi r^2 = 177 \text{ in}^2$$

$$S = \frac{\pi r^3}{4} = 331 \text{ in}^3$$

$$I = \frac{\pi r^4}{4} = 2485 \text{ in}^4$$

#### 2. Required pile penetration (Section 7-3.02A)

$$\text{Minimum } \frac{D}{H} = 0.75; \text{ design } \frac{D}{H} = \frac{14}{16} = 0.875 \quad \underline{\text{OK}}$$

$$\text{Minimum } D \text{ for construction} = (0.75 \times 16.0) = 12.0'$$

#### 3. Soil relaxation factor (Section 7-3.02D)

Assumptions: (1) normal (average) soil

(2) 30-day time period

From Soil Factor Chart (Figure 7-12)  $R = 1.25$

#### 4. Point of pile fixity (Section 7-3.02B)

$$Y_1 = (4 \times \text{ground line pile diameter}) = (4 \times 1.25) = 5.0'$$

$$Y_2 = (Y_1 \times \text{soil relax. factor}) = (5.0 \times 1.25) = 6.25'$$

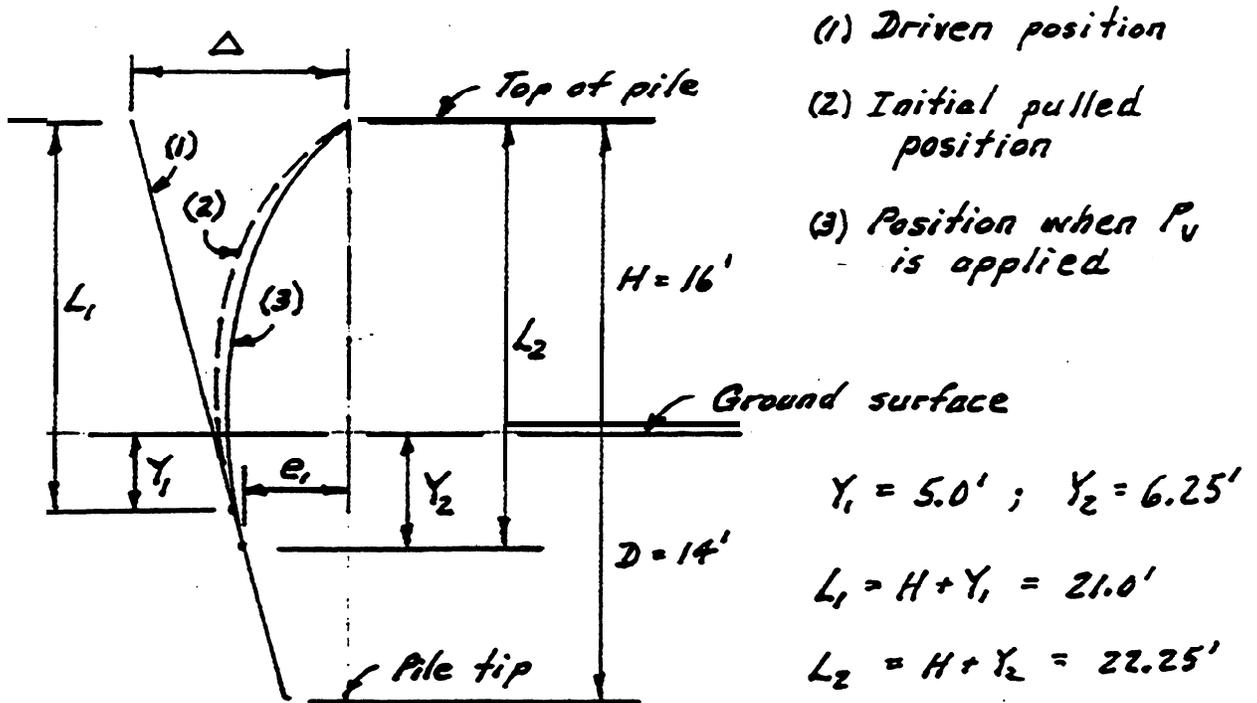
5. Driving tolerances (Section 7-3.02C)

Max. pile pull =  $\Delta = 6''$   
 Max. pile lean =  $e_1 = 4''$  } from F/W drawings

6. Modulus of elasticity (Section 7-3.02E)

Assume  $E = 1,600,000$  psi

Effect of Pile Pull (Section 7-3.03A)



Pile Schematic (no scale)

1. Calculate force to pull pile into line

$$F_1 = \frac{3EI\Delta}{(12L)^3} = \frac{3(1.6 \times 10^6)(2485)(6)}{(12 \times 21.0)^3} = 4472 \text{ lbs.}$$

2. Calculate the initial bending stress

$$f_{bp(1)} = \frac{(F_1)(12L_1)}{S} = \frac{(4472)(12 \times 21.0)}{391} = 3405 \text{ psi}$$

3405 psi < 4000 psi allowed - OK

## Pile Pull Continued

3. Calculate force remaining when  $P_u$  is applied

$$F_2 = \frac{F_1 (L_1)^3}{(L_2)^3} = \frac{4472 (21.0)^3}{(22.25)^3} = 3760 \text{ lbs.}$$

4. Calculate relaxed bending stress

$$f_{bp(2)} = \frac{F_2 (12L_2)}{S} = \frac{3760 (12 \times 22.25)}{331} = 3033 \text{ psi}$$

## Evaluate System Adequacy (Section 3.03E)

1. Determine bent type

$$L_u = \frac{1}{2} + (16.0 - 10.0) = 6.25 + 6.0 = 12.25'$$

$$L_u/d = \frac{12.25}{1.25} = 9.8 \quad \therefore \text{Type II bent}$$

Consider H but not P-delta (Section 7-3.03C)

2. Calculate stress due to pile lean

$$f_{be(1)} = \frac{P_v (e_1)}{S} = \frac{36000 (4)}{331} = 435 \text{ psi}$$

3. Calculate stress due to design H

$$H = (0.02 \times 36000) = 720 \text{ lbs.}$$

$$f_{bH} = \frac{(H)(12L_u)}{S} = \frac{(720)(12.25 \times 12)}{331} = 320 \text{ psi}$$

4. Calculate horiz. displacement

$$x = \frac{H(12L_u)^3}{3EI} = \frac{720(12 \times 12.25)^3}{3(1.6 \times 10^6)(2485)} = 0.19'' = e_2$$

5. Calculate stress due to additional  $P_v$  eccentricity

$$f_{be(2)} = \frac{P_v (e_2)}{S} = \frac{36000 (0.19)}{331} = 21 \text{ psi}$$

## System Adequacy Continued

5. Calculate stress due to axial compression

$$f_c = \frac{P_v}{A} = \frac{36000}{177} = 203 \text{ psi}$$

6. Determine allowable compressive stress

Bent is supported at the cap in the longitudinal direction.

$$L_u \text{ (in longitudinal direction)} = L_2 = 22.25'$$

$$\text{Equivalent "d"} = \sqrt{A} = \sqrt{177} = 13.3''$$

$$L_u/d = \frac{12 \times 22.25}{13.3} = 20.1$$

$$F_c = \frac{480,000}{(20.1)^2} = 1188 \text{ psi}$$

7. Check pile adequacy using combined stress expression

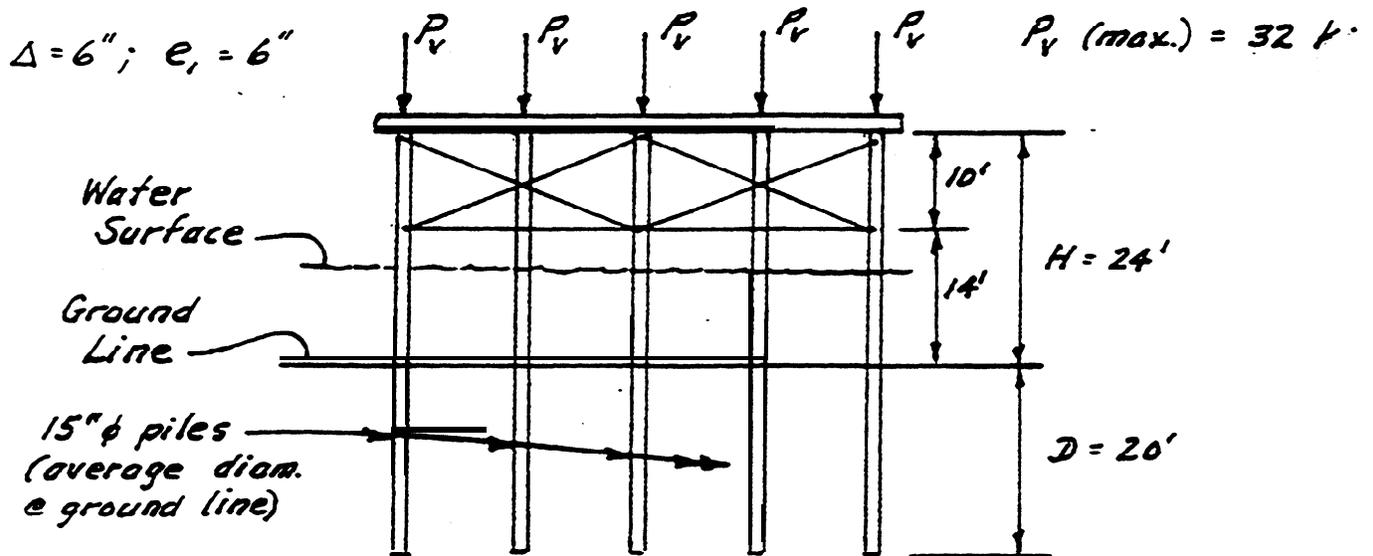
$$\frac{f_{p(c)} + 2f_{b(c)} + 2(f_{bH} + f_{b(c)})}{3F_b} + \frac{2f_c}{3F_c} \leq 1.0$$

$$\frac{3033 + 2(435) + 2(320 + 21)}{3(1800)} + \frac{2(203)}{3(1188)}$$

$$0.85 + 0.11 = 0.96$$

System is adequate

## Example 14C (Type III Bent)



### Preliminary Calculations and Assumptions

#### 1. Pile properties (15" $\phi$ pile; $r = 7.5''$ )

$$A = \pi r^2 = 177 \text{ in}^2$$

$$S = \pi r^3 / 4 = 331 \text{ in}^3$$

$$I = \pi r^4 / 4 = 2485 \text{ in}^4$$

#### 2. Required pile penetration (Section 7-3.02A)

$$\text{Minimum } D/H = 0.75; \text{ design } D/H = 20/24 = 0.83 \quad \underline{\text{OK}}$$

$$\text{Minimum } D \text{ for construction} = (0.75)(24) = 18.0'$$

#### 3. Soil relaxation factor (Section 7-3.02D)

Assumptions: (1) normal (average) soil

(2) 30-day time period

$$\text{From Soil Factor Chart (Figure 7-12)} \quad R = 1.25$$

#### 4. Point of pile fixity (Section 7-3.02B)

$$Y_1 = (4 \times \text{ground line pile diam.}) = (4 \times 1.25) = 5.0'$$

$$Y_2 = (Y_1 \times \text{soil relax. factor}) = (5.0 \times 1.25) = 6.25'$$

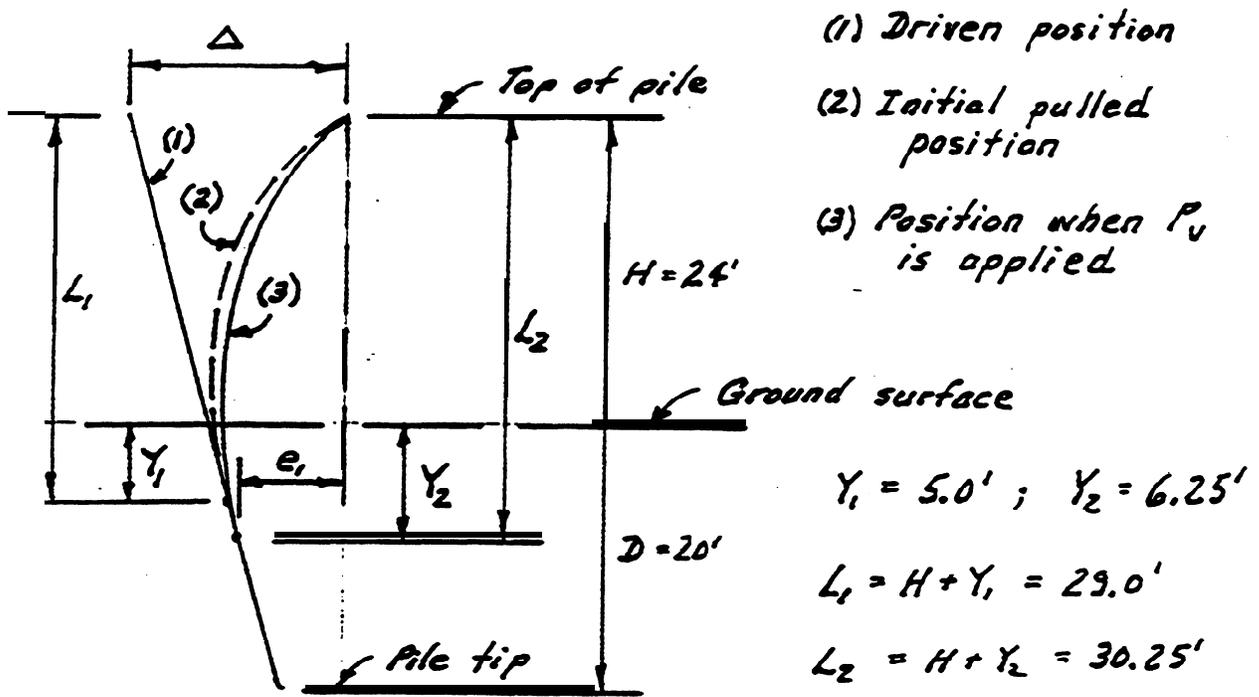
5. Driving tolerances (Section 7-3.02C)

Max. pile pull =  $\Delta = 6''$   
 Max. pile lean =  $e_1 = 6''$  } values from F/W drawings

6. Modulus of elasticity (Section 7-3.02E)

Assume  $E = 1,600,000$  psi

Effect of Pile Pull (Section 7-3.03A)



Pile Schematic (no scale)

1. Calculate force to pull pile into line

$$F_1 = \frac{3EI\Delta}{(12L_1)^3} = \frac{3(1.6 \times 10^6)(2485)(6)}{(12 \times 29.0)^3} = 1698 \text{ lbs.}$$

2. Calculate the initial bending stress

$$f_{bp(1)} = \frac{F_1(12L_1)}{S} = \frac{(1698)(12 \times 29.0)}{331} = 1785 \text{ psi}$$

1785 < 4000 psi allowed - OK

## Pile Pull Continued

3. Calculate force remaining when  $P_v$  is applied

$$F_2 = \frac{F_1 (L_1)^3}{(L_2)^3} = \frac{(1698 \times 29.0)^3}{(30.25)^3} = 1496 \text{ lbs}$$

4. Calculate the relaxed bending stress

$$f_{bp(z)} = \frac{F_2 (12 L_2)}{S} = \frac{(1496 \times 12 \times 30.25)}{331} = 1640 \text{ psi}$$

## Evaluate System Adequacy (Section 7-3.03E)

1. Determine bent type

$$L_u = Y_2 + (24.0 - 10.0) = 6.25 + 14.0 = 20.25'$$

$$L_u/d = \frac{20.25}{1.25} = 16.2 > 15, \therefore \text{Type III Bent}$$

Consider P-delta effect (Section 7-3.03D)

2. Calculate stress due to pile lean

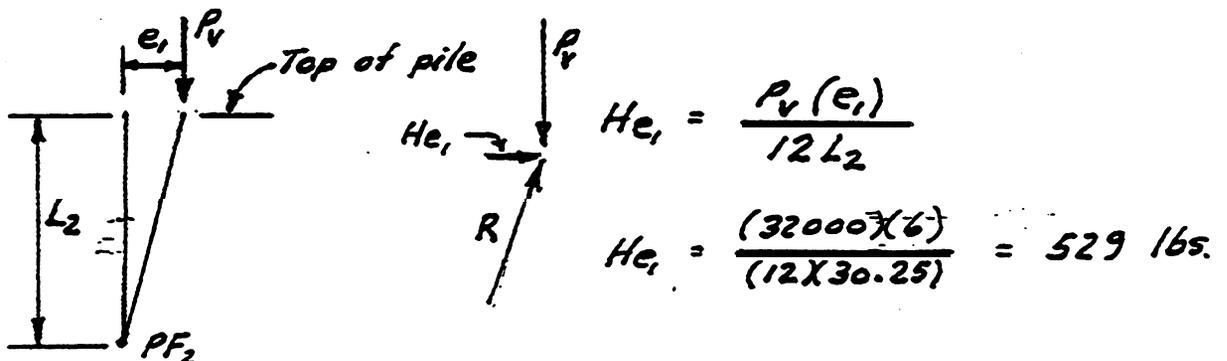
$$f_{be} = \frac{P_v (e_1)}{S} = \frac{(32000 \times 6)}{331} = 580 \text{ psi}$$

3. Calculate stress due to design H

$$H = (0.02 \times 32,000) = 640 \text{ lbs.}$$

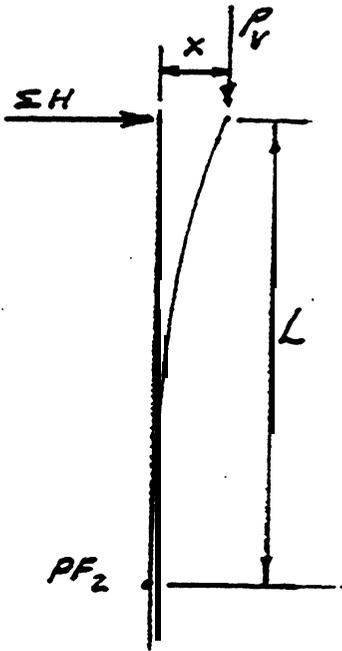
$$f_{bH} = \frac{H (12 \times L_u)}{S} = \frac{(640 \times 12 \times 20.25)}{331} = 470 \text{ psi}$$

4. Calculate horizontal component of  $P_v$  reaction



## System Adequacy Continued

### 5. Calculate total horizontal displacement ( $e_3$ )



$x$  = displacement due to total H load

$$x = \frac{\Sigma H (L)^3}{3EI}$$

$$\begin{aligned} \Sigma H &= \text{design H} + H_e \\ &= 640 + 529 = 1169 \text{ lbs.} \end{aligned}$$

$$L = \frac{1}{2} + (24 - 10) = 20.25' = 243''$$

$$\begin{aligned} 3EI &= 3(1.6 \times 10^6 \times 2485) \\ &= 1.193 \times 10^{10} \end{aligned}$$

Refer to Section 7-3.03D and Figure 7-15

$$x = \frac{(1169 \times 243)^3}{3EI} = 1.41''$$

$$H_1 = 1169 + \frac{(32000 \times 1.41)}{243} = 1355 \text{ lbs.}$$

$$x_1 = \frac{(1355 \times 243)^3}{3EI} = 1.63''$$

$$H_2 = 1355 + \frac{(32000 \times (1.63 - 1.41))}{243} = 1384 \text{ lbs.}$$

$$x_2 = \frac{(1384 \times 243)^3}{3EI} = 1.66''$$

Values within 5% STOP

### 6. Calculate bending stress due to $\Sigma H$ displacement

$$f_{be_3} = \frac{P_v (e_3)}{S} = \frac{(32000 \times 1.66)}{331} = 160 \text{ psi}$$

### 7. Calculate stress due to axial compression

$$f_c = \frac{P_v}{A} = \frac{32000}{177} = 181 \text{ psi}$$

## System Adequacy Continued

### 8. Determine allowable compressive stress

Bent is supported at the cap in the longitudinal direction.

$$L_u \text{ (in longitudinal direction)} = L_2 = 30.25'$$

$$\text{Equivalent "d"} = \sqrt{A} = \sqrt{177} = 13.3''$$

$$L_u/d = \frac{12 \times 30.25}{13.3} = 27.3$$

$$F_c = \frac{480000}{(27.3)^2} = 644 \text{ psi}$$

### 9. Check pile adequacy using combined stress expression

$$\frac{f_{bp(2)} + 2f_{bc(1)} + 2(f_{bt} + f_{bc(2)})}{3F_b} + \frac{2f_c}{3F_c} \not\geq 1.0$$

$$\frac{1640 + 2(580) + 2(470 + 160)}{3(1800)} + \frac{2(181)}{3(644)}$$

$$0.75 + 0.19 = 0.94$$

System is adequate